



## Research Article

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# Task Planning for Transportation of Multiple Objects by Dual Robots Using Cloud Computing

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## Abstract

In this paper, the application of cloud computing in the field of robotics is described. Dual robots are assigned the job of picking up objects lying on the floor and to keep them in the given spaces. In the co-operative environment both the robots try to follow their route of shortest path till such situations arise when either the object or the space has been exhausted. Then the robot searches for the next nearest object or space or the remaining object or space and act accordingly. Due to simultaneous movement of the dual robots, there may be collision between the two robots. Detection of whether there is any collision or not is also described.

## Keywords

Cloud Computing, Cooperative Environment, Dual robots, Object, Shortest Path

## Introduction

The key reason of utilizing robots in industry is improving the production efficiency. The efficiency depends upon the production process which again depends upon the movement of the robots. Therefore, a lot of efforts are given for making robots more productive: Making efficient control [1], optimizing trajectories by optimizing velocity profiles [2] or end-effector path [3], and planning collision-free paths [4]. Mostly these approaches are movement oriented. However, there are problems consisting of a number of tasks and the robot's applications in industry is to sequence them for optimization of path or resources. The easiest way to solve the task sequencing problem is to model it as the Traveling Salesman Problem (TSP) [5]. The goal of the TSP is to find a minimal-cost cyclic tour through a set of points such that every point is visited once. Multi-goal planning is another problem that considers obstacles in the environment; therefore, a collision-free path is the output. Task sequencing/scheduling [6,7] may or may not consider obstacles, therefore, the output in either case is a sequence or a path. There are several recent surveys that cover the related domains, e.g., multi-robot patrolling algorithms [8], assembly process planning [9], methods to solve Traveling Salesman Problem [10] and coverage path planning for robotics [11]. This paper provides a related combinatorial TSP-like problem that is applied in robot task sequencing.

In multiple robots task planning, the tasks have to be distributed among robots. One of the first to address this problem was Maimon [12]. He proposed the robot task-sequencing planning problem. Later, Zhang, et al. [13] proposed the

approach for task allocation for a team of robots. The Stochastic Clustering Auction technique by Zhang, et al. [14] was used in this approach. This optimizes using the greedy principal, making worse steps for avoiding the local minima. The general principal is to re-cluster the tasks until termination condition is satisfied. If the cluster is better than the previous one, then it is accepted as the current one, by following Simulated Annealing strategy.

The task-level planning defines the robot actions by their interactions with objects. Often the final goal is known. The task level planning has to find a sequence of actions that a robot has to perform to change the environment from the initial state to the goal state. Every single action is then planned with domain dependent planner. Cao, et al. [15] proposed a net called AND/OR used for reasoning about geometrical task constraints. The general idea is to map proposed net to Petri net. Then, the solution search is performed by building a reachability tree from the Petri net. Later, Chien, et al. [16,17] proposed the efficient way to incorporate the domain information into the planner for the indoor robot scenario. The

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data is represented with object-oriented model. This model includes relation between objects, categories and physical laws. Task-level planning was also applied to mobile robotics by Galindo, et al. [18], where the hierarchical planning technique was proposed to reduce the computational expenses. In task sequencing, the tasks are areas that have to be visited, but not the objects with its handling features as in task-level planning. However, task sequencing problem may allow partial order of the sequence.

Often, researchers observe task-level and path planning as a separate problem. However, in real life, the plan created by the task-level planner often cannot be executed due to the failure of the path-planner. In that case, the task-level planner has to construct a new plan. Therefore, it is essential to design a task-level planner in combination with a collision-free planner. Bhatia, et al. [19] proposed the architecture that allows combining task-level planning with low-level motion planning by introducing new synergy level. Gaschler, et al. [20] proposed the knowledge volume approach. The main idea was to make an intermediate stage between continuous robot motions and symbolic planning.

In 2010, the term “Cloud Robotics” was introduced by James Kuffner at Google to describe how the Internet helps in massively parallel computation and sharing of vast data resources [21]. It is very much related to earlier work on “Remote Brained” robots [22]. It is for this type of connectedness that Steve Cousins, former CEO of Willow Garage, conceptualized the statement: “No robot is an island.” The autonomous car built by Google exemplifies the idea. It utilizes maps and images collected and updated by satellite, Street-view, and crowd-sourcing from the network to facilitate accurate localization. Kar, et al. [23] utilized the concept of cloud in Task planning and sequencing for single robot without any constraint, with priority constraints [24] and particular jobs in particular spaces constraints [25]. Kar, et al. then extended the concept of cloud in Task planning and sequencing for dual robots without any constraint [26], with particular jobs in particular spaces constraints [27,28] and priority constraints [29,30].

After studying the above-mentioned papers we can conclude that by developing Task-planning algorithm using Cloud computing, we can make the robots perform the tasks and we can simulate the environment through some programming language to graphically show the traversal of the robots. We can even develop an algorithm to prevent the robots from colliding with each other. To the best of our knowledge, there is no research work that covers the task sequencing problem for dual robots using Cloud computing.

## Problem Definition

Dual robots have been assigned the work of picking up multiple objects from a plane area and placing them in some given spaces without any constraints. A separate computer system will communicate with both the robots and determines the routes from the locations of the robots, the objects and the spaces. Cloud Computing can be used for this purpose. The problem is to find the routes for the robots for

performing the tasks in the shortest possible time.

The object that lies at the minimum distance of the starting point of each robot is to be found out by calculating the distances of all the objects from each robot. If the same object is at the minimum distance from each of the two robots then the robot that is at minimum distance from the object will go for the object and the other robot will go for the object that is at the next minimum distance from it. When one robot picks up an object, it will keep the object in the space that is nearest to it and empty. When one robot reaches a particular space and keeps the object there, it will go for the next object that is nearest to it and not picked up by any robot. The process is repeated till all the objects are picked up and placed.

## Methodology of Solving the Problem

### Assumptions for the work

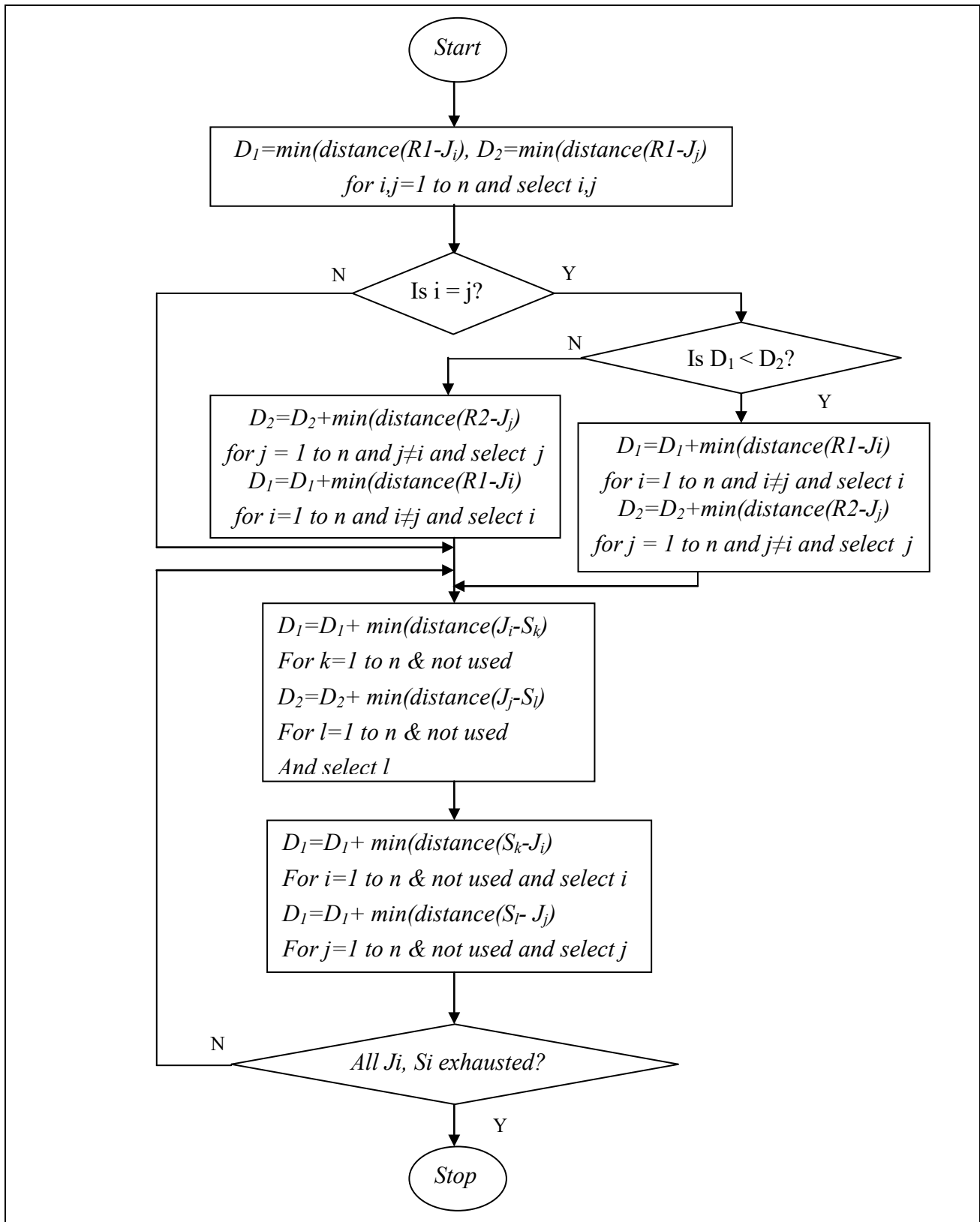
- i. Both the robots are assumed to be point robots (i.e. with negligible dimensions).
- ii. Four objects and four spaces are taken as a case study.
- iii. Objects may be picked up in any order.
- iv. Only one object can be placed at one space.
- v. Any object may be placed at any space.
- vi. Both the robots will start at the same time and move with same speed.
- vii. Both the robots are initially at reasonably close distances from the objects.
- viii. The time for picking up an object from source and placing the object at the destination by the robot is negligible.
- ix. The initial location of Robot1 is assumed to be the origin and is denoted by R1.
- x. The initial location of Robot2 is assumed as (120, 0) and is denoted by R2.

### Algorithm: Stage by stage minimum distance

The object that lies at the minimum distance of the starting point of each robot is to be found out by calculating the distances of all the objects from each robot. If the same object is at the minimum distance from each of the two robots then the robot that is at minimum distance from the object will go for the object and the other robot will go for the object which is at the next minimum distance. When one robot picks up an object, it will keep the object in the space that is nearest to it and empty. When one robot reaches a particular space and keeps the object there, it will go for the next object that is nearest to it and not picked up by any robot. The process is repeated till all the objects are picked up and placed.

Let  $R1$  and  $R2$  denote the initial position of robot1 and robot2,  
 $J_i$  denote the location of the objects  $i$ ,  
 $S_i$  denote the location of the space  $i$ .  
(1)  $D_1 = \min(\text{distance}(R1-J_i))$  for all  $i$   
from 1 to  $n$   
 $D_2 = \min(\text{distance}(R2-J_j))$  for all  $j$  from 1 to  $n$   
If  $i = j$  then, Calculate  
 $D = \min(D_1, D_2)$   
If  $D_1 > D_2$  then,  
 $D_2 = D$   
 $D_1 = \min(\text{distance}(R1-J_i))$  for all  $i$  from 1 to  $n$  such that  $i \neq j$   
Else  
 $D_1 = D$   
 $D_2 = \min(\text{distance}(R2-J_j))$  for all  $j$  from 1 to  $n$  such that  $j \neq i$   
End if;  
End if;  
(2) (i)  $D_1 = D_1 + \min(\text{distance}(J_i-S_k))$   
for  $k$  from 1 to  $n$  and  $i$  selected in (1)  
 $D_2 = D_2 + \min(\text{distance}(J_j-S_l))$  for  $l$  from  $n$  and  $j$  selected in (1)  
and for  $l \neq k$   
(ii)  $D_1 = D_1 + \min(\text{distance}(S_k-J_l))$   
for  $l$  from 1 to  $n$  and  $k$  selected in 2(i)  
 $D_2 = D_2 + \min(\text{distance}(S_l-J_i))$   
for  $k$  from 1 to  $n$  and  $k$  selected in 2(i) and for  $i \neq j$   
(3) Repeat Step 2 until all the objects and  
the spaces are exhausted.

Algorithm: Stage by Stage Minimum Distance



Flowchart for the algorithm: Stage by stage minimum distance

#### Demonstration of the algorithm with test case 1

For demonstration of the algorithm with a Test Case, four objects are considered, which are to be kept at four spaces. The current location of the objects are denoted by  $J_i$  where  $i = 1$  to 4 and the locations where the objects are to be kept are denoted by  $S_i$  where  $i = 1$  to 4. In the Test Case, the locations of objects and spaces are shown in Table 1 and Table 2.

The layout of the workspace showing the locations of the robots, the objects and the spaces are represented in the Figure 1.

As shown in Figure 1, the initial positions of the robots Robot1 is (0,0) and Robot2 is (120,0). As both the robots are assumed to move with same speed, the routes of the robots can be determined on the basis of distances traversed by them to reach the objects or the spaces. The distance matrix for R1 and R2 is given in the Table 3.

The two robots are working simultaneously. The path of both the robots along with the distances at each stage of operation and the cumulative distances are calculated are given below:

At the beginning,  $D_1 = 10.82(R1-J2)$  and  $D_2 = 58.31(R2-J3)$ . So, Robot1 moves to J2 and Robot2 moves to J3. From J2, S1 is nearest, Robot1 moves to S1 to keep the object. From J3, S3 and S4 are nearest. Robot2 chooses S4 (or S3) to keep it. From S1, J4 is nearest, Robot1 moves to J4 to pick it up. From S4 (or S3), J1 is nearest, Robot2 moves to J1 to pick it up.

From J1, S3 (or S4) is nearest, Robot2 moves to keep the object at S3 (or S4). From J4, only S2 is lying vacant and so Robot1 has no other choice but to keep the object at S2.

Thus the routes of the robots are:

R1-J2-S1-J4-S2 and R2-J3-S4-J1-S3 or

R1-J2-S1-J4-S2 and R2-J3-S3-J1-S4

**Table 1:** Location of different objects.

Objects	X	Y
J1	99	77
J2	9	6
J3	70	30
J4	88	62

The routes of the two robots along with the distance at each stage and the cumulative distances are calculated and shown in Table 4a and Table 4b for the two cases.

So, the objects will be kept at spaces as show in Table 5.

The steps of the robot movement obtained by the program are shown in Figure 2 for the case discussed. The graphical view of the path of the two robots is given in the Figure 3.

### Demonstration of the algorithm with test case 2

The program has been tested for another case with different object locations. Some cases with results are shown in Table 6, Table 7, Table 8 and Table 9, Figure 4 and Figure 5.

**Table 2:** Location of spaces.

Spaces	X	Y
S1	20	100
S2	40	100
S3	60	100
S4	80	100

**Table 3:** distance of the objects from the robots and the spaces.

	J1	J2	J3	J4
R1	125.42	10.82	76.16	107.65
R2	79.81	111.16	58.31	69.77
S1	82.28	94.64	86.02	77.90
S2	63.32	98.98	76.16	61.22
S3	45.28	106.94	70.71	47.20
S4	29.83	117.80	70.71	38.83

**Table 4a:** Path of Robot1 & Robot2 along with distance and cumulative distance.

Obj	Dist	Cu. Dist	Obj	Dist.	Cu. Dist	Robot1	Robot2	Min.
R1-J2	10.82	10.82	R2-J3	58.31	58.31	10.82	58.31	10.82
J2-S1	94.64	105.46				105.46	58.31	58.31
			J3-S4	70.71	129.02	105.46	129.02	105.46
S1-J4	77.9	183.36				183.36	129.02	129.02
			S4-J1	29.83	158.85	183.36	158.85	158.85
			J1-S3	45.28	204.13	183.36	----	183.36
J4-S2	61.22	244.58						

**Table 4b:** Path of Robot1 & Robot2 along with distance and cumulative distance.

Obj	Dist.	Cu. Dist	Obj	Dist.	Cu. Dist	Robot1	Robot2	Min.
R1-J2	10.82	10.82	R2-J3	58.31	58.31	10.82	58.31	10.83
J2-S1	94.64	105.46				105.46	58.31	58.31
			J3-S3	70.71	129.02	105.46	129.02	105.46
S1-J4	77.9	183.36				183.36	129.02	129.02
			S3-J1	45.28	174.3	183.36	174.3	174.3
			J1-S4	29.83	204.13	183.36	----	183.36
J4-S2	61.22	244.58						

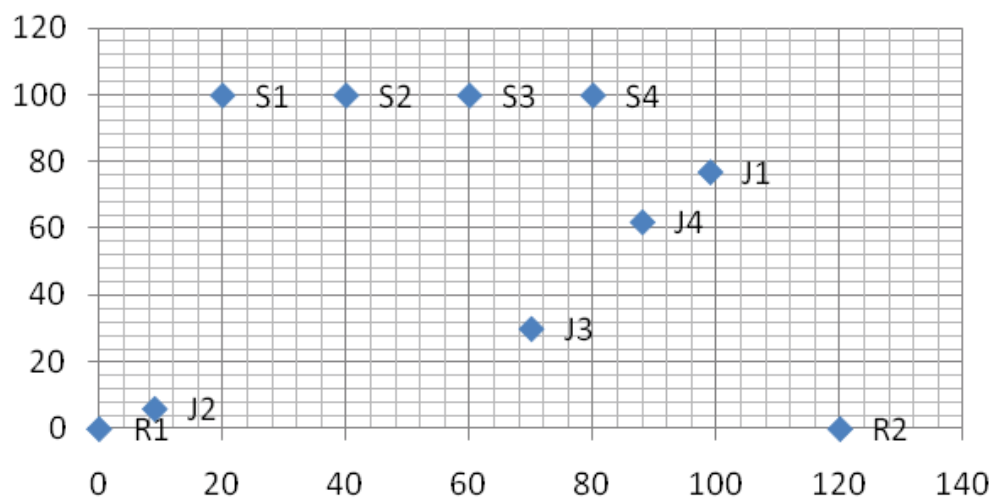


Figure 1: Layout showing the location of the robots, the objects and the spaces.

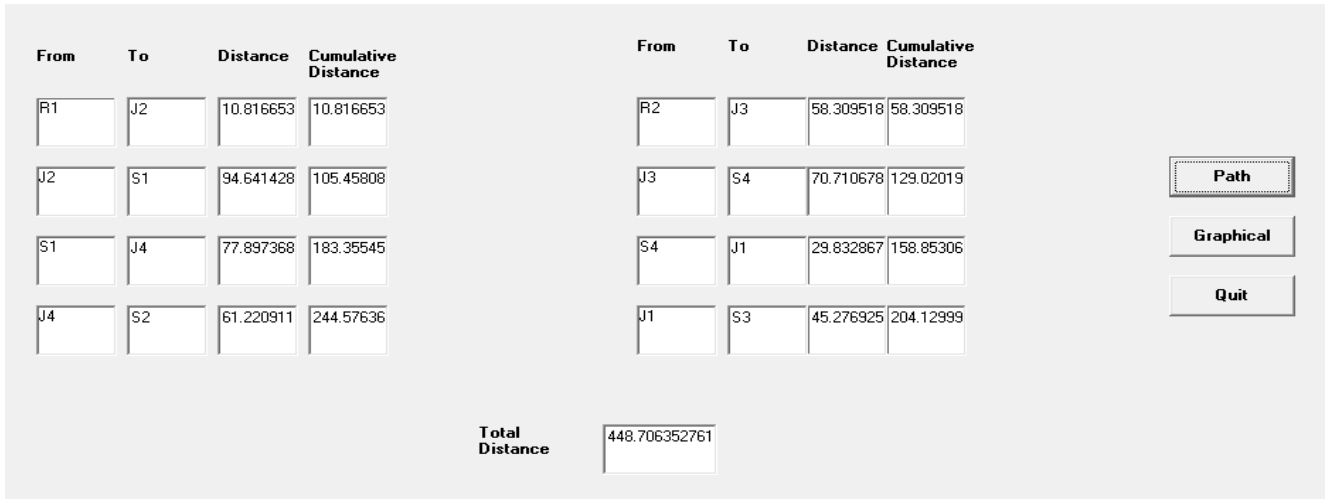


Figure 2: Paths of robot1 & robot2.

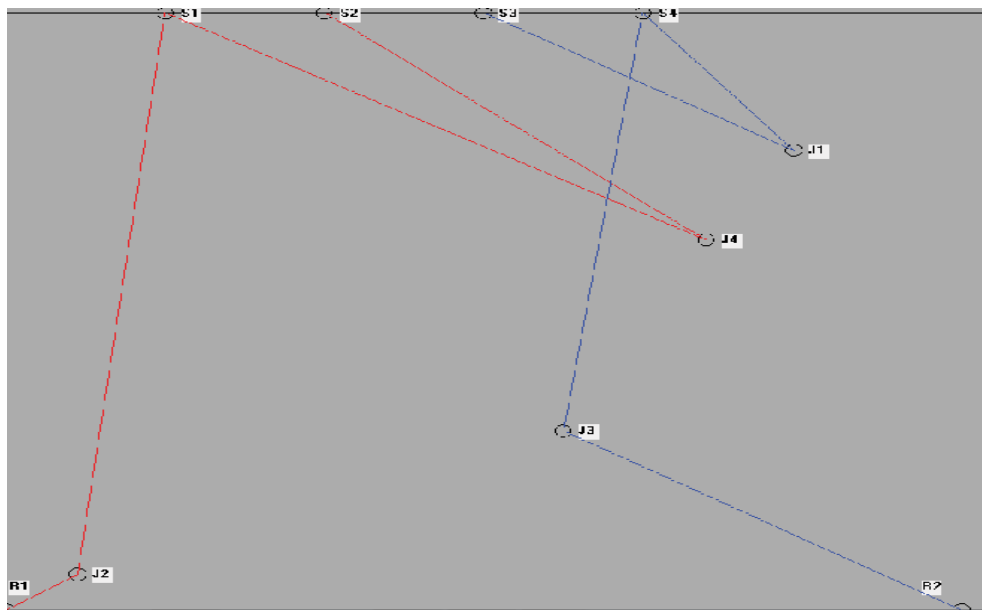


Figure 3: Graphical representation of the paths of robot1 (by red lines) and robot2 (by blue lines).

**Table 5:** Objects kept in spaces by the robots.

Object	Space	Done by
J2	S1	R1
J3	S4	R2
J1	S3	R2
J4	S2	R1

**Table 7:** distance of the objects from the robots and the spaces.

	J1	J2	J3	J4
R1	107.1168	133.2554	90.82401	86.68333
R2	13.92839	69.26038	111.036	126.1507
S1	128.8177	98.9798	30.4795	17.72005
S2	116.2497	80.23092	20.22375	22.67157
S3	105.9906	62.26556	26.24881	38.91015
S4	98.76234	46.01087	42.05948	57.56735

**Table 6:** Location of objects.

Object	X	Y
J1	107	5
J2	114	69
J3	43	80
J4	25	83

**Table 8:** Path of Robot1 & Robot2 along with distance and cumulative distance.

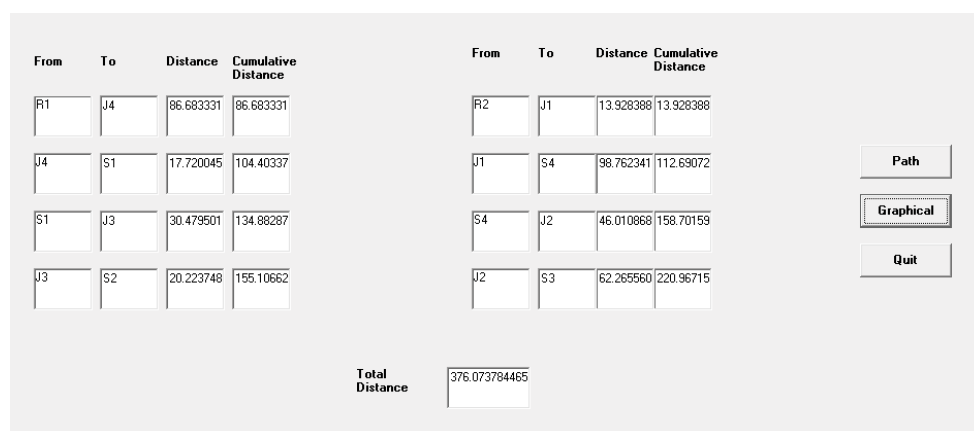
Obj	Dist	Cu. Dist	Obj	Dist.	Cu. Dist	Robot1	Robot2	Min.
R1-J4	86.68	86.68	R2-J1	13.93	13.93	86.68	13.93	13.93
			J1-S4	98.76	112.69	86.68	112.69	86.68
J4-S1	17.72	104.4				104.4	112.69	104.4
S1-J3	30.48	134.88				138.88	112.69	112.69
			S4-J2	46.01	158.7	138.88	158.7	138.88
J3-S2	20.22	155.11				----	158.7	158.7
			J2-S3	62.27	220.97			

**Table 9:** Objects kept in spaces by the robots.

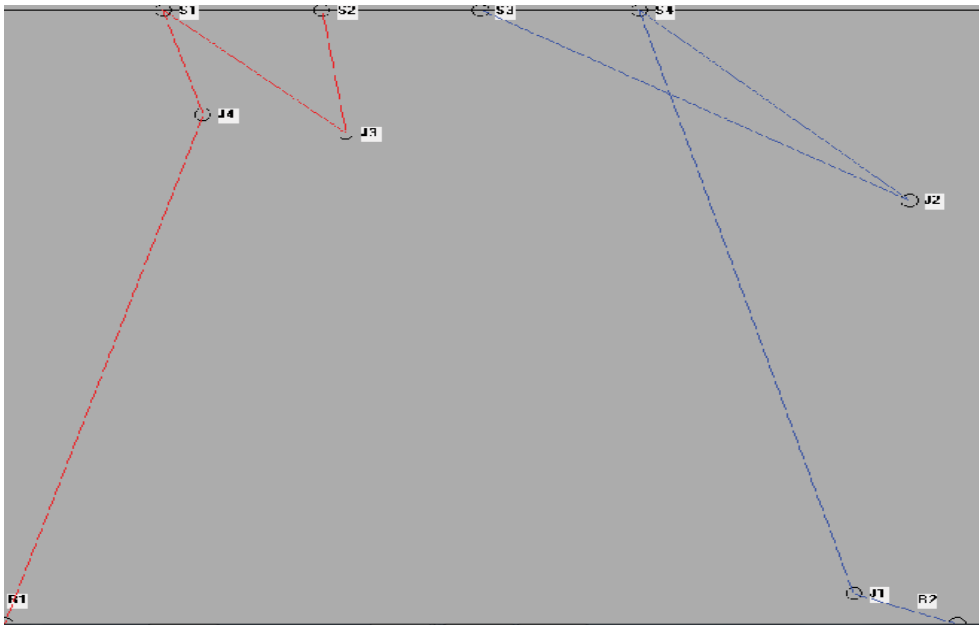
Object	Space	Done by
J1	S4	R1
J4	S1	R2
J3	S2	R2
J2	S3	R1

**Table 10:** Location of objects.

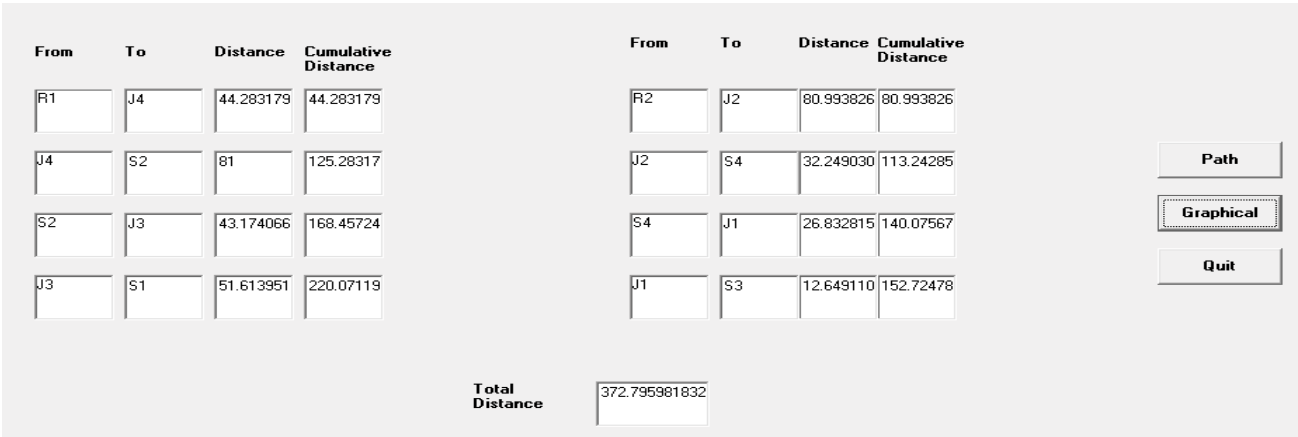
Object	X	Y
J1	56	88
J2	76	68
J3	50	58
J4	40	19



**Figure 4:** Paths of robot1 and robot2.



**Figure 5:** Graphical representation of paths of robot1 (by red lines) and robot2 (by blue lines).



**Figure 6:** Paths of robot1 and robot2.

**Table 11:** distance of the objects from the robots and the spaces.

	J1	J2	J3	J4
R1	104.3072	101.9804	76.57676	44.28318
R2	108.8118	80.99383	90.90655	82.2253
S1	37.94733	64.49806	51.61395	83.43261
S2	20	48.16638	43.17407	81
S3	12.64911	35.77709	43.17407	83.43261
S4	26.83282	32.24903	51.61395	90.33825



Table 12: Path of Robot1 & Robot2 along with distance and cumulative distance.

Obj	Dist	Cu. Dist	Obj	Dist.	Cu. Dist	Robot1	Robot2	Min.
R1-J4	44.28	44.28	R2-J2	80.99	80.99	44.28	80.99	44.28
J4-S2	81	125.28				125.28	80.99	80.99
			J2-S4	32.25	113.24	125.28	113.24	113.24
			S4-J1	26.83	140.08	125.28	140.08	125.28
S2-J3	43.17	168.46				168.46	140.08	140.08
			J1-S3	12.65	152.72	168.46	----	168.46
J3-S1	51.61	220.07						

Table 13: Objects kept in spaces by the robots.

Object	Space	Done by
J4	S2	R1
J2	S4	R2
J1	S3	R2
J3	S1	R1

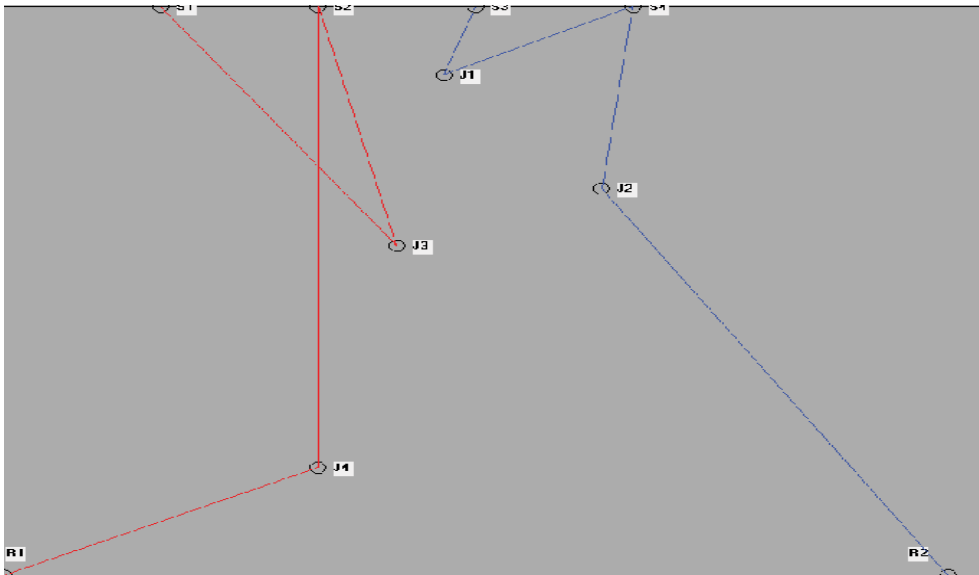


Figure 7: Graphical representation of the paths of robot1 (by red lines) and robot2 (by blue lines).

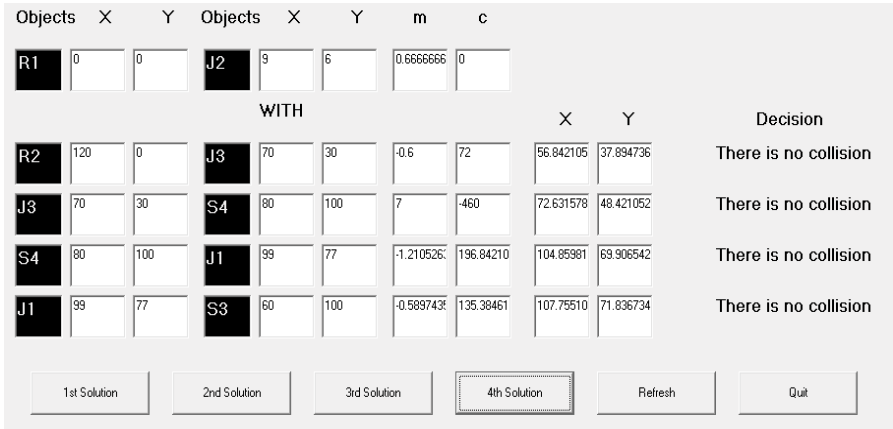


Figure 8: Collision detection between R1J2 with R2J3, J3S4, S4J1 and J1S3.

### Demonstration of the algorithm with test case 3

Another case with results is shown in Table 10, Table 11, Table 12 and Table 13, Figure 6 and Figure 7.

### Algorithm: Detection of collision

*The point of intersection of the lines, that robot1 and robot2 traverses, can be found out.*

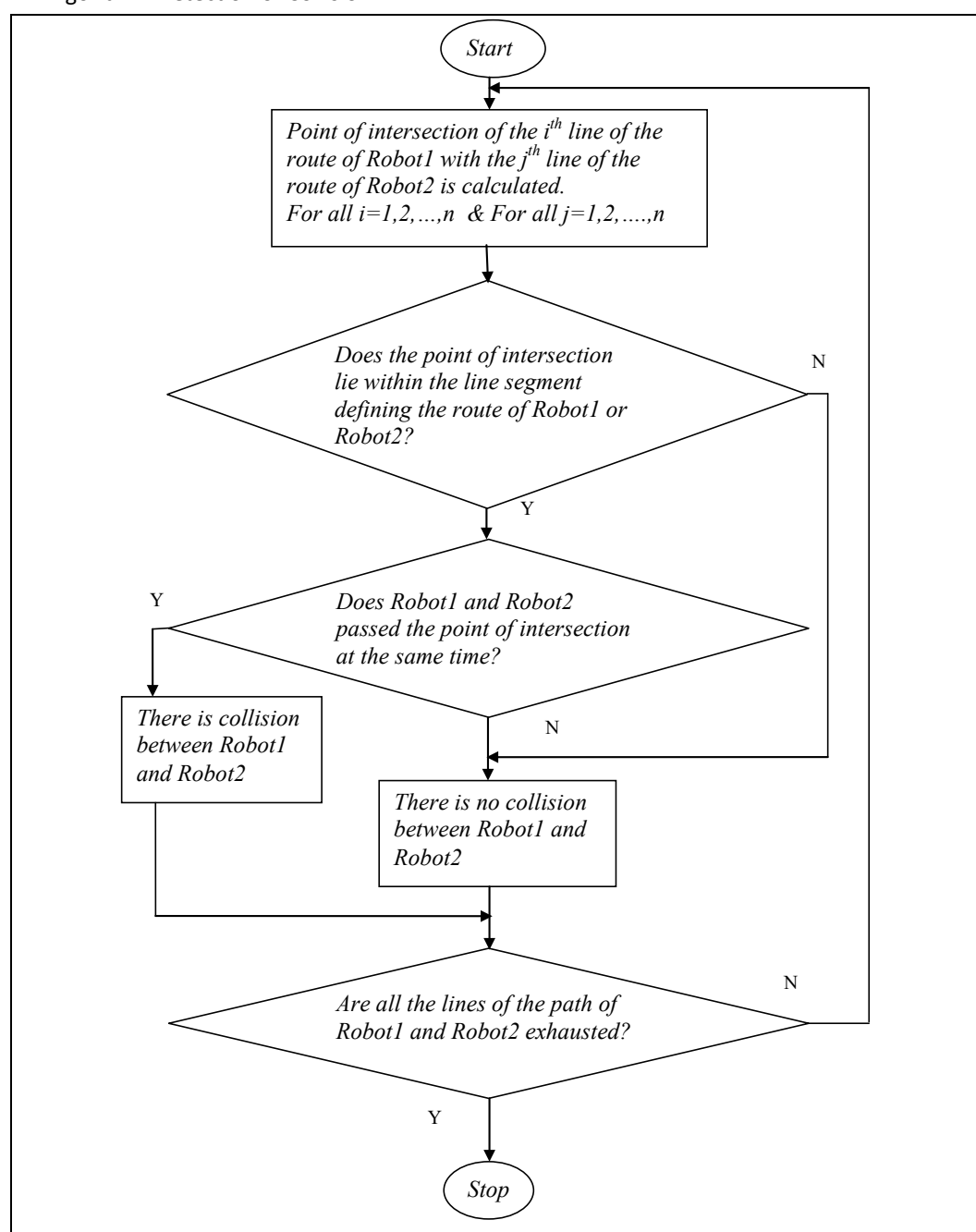
*If the point of intersection lies within the two line segments, then there is possibility of a collision. Then, the time of crossing of the point by the two robots are to be calculated.*

*If the times of crossing of the two robots are not significantly different from each other, then there is collision.*

*Else, if the times of crossing of the two robots are significantly different from each other, then there is no collision.*

*Else, there is no collision.*

Algorithm: Detection of Collision



Flowchart for the Algorithm: Detection of Collision

### Demonstration of the algorithm with test case 1

The robot1 traverses the path R1-J2-S1-J4-S2. It moves through the line segments R1-J2, J2-S1, S1-J4 and J4-S2. The robot2 traverses the path R2-J3-S4-J1-S3. It moves through the line segments R2-J3, J3-S4, S4-J1 and J1-S3. We compare each line segment of the path of robot1 with each line segment of the path of robot2 for intersection.

From Figure 8, it is found that the line R1-J2 will intersect the line R2-J3 at the point (56.84, 37.89) which does not lie between the points R1 and J2. So there is no collision.

The line R1-J2 will intersect the line J3-S4 at the point (72.63, 48.42) which does not lie between the points R1 and J2. So there is no collision.

The line R1-J2 will intersect the line S4-J1 at the point (104.86, 69.91) which does not lie between the points R1 and J2. So there is no collision.

The line R1-J2 will intersect the line J1-S3 at the point (107.76, 71.84) which does not lie between the points R1 and J2. So there is no collision.

From Figure 9, it is found that the line J2-S1 will intersect the line R2-J3 at the point (15.62, 62.62) which does not lie between the points R2 and J3. So there is no collision.

The line J2-S1 will intersect the line J3-S4 at the point (-251.76, -2222.35) which does not lie between the points J2 and S1. So there is no collision.

The line J2-S1 will intersect the line S4-J1 at the point (27.44, 163.62) which does not lie within the points J2 and S1. So there is no collision.

The line J2-S1 will intersect the line J1-S3 at the point (22.58, 122.07) which does not lie within the points J2 and S1. So there is no collision.

From Figure 10, it is found that the line S1-J4 will intersect the line R2-J3 at the point (-951.43, 642.86) which does not lie between the points R2 and J3. So there is no collision.

The line S1-J4 will intersect the line J3-S4 at the point (75.56, 68.95) which lies between the points J3 and S4 and between the points S1 and J4. So it cannot be concluded that there is no collision.

Let M be the point of intersection of S1-J4 and J3-S4. Location of M is (75.56, 68.95) (from Figure 10).

$$\text{Distance of M from S1 is } \sqrt{(75.56 - 20)^2 + (68.95 - 100)^2} = 63.65 \text{ units}$$

Robot1 reached S1 covering a distance of 105.46 units (from Figure 2). For reaching M, Robot1 has to cover 105.46 + 63.65 = 169.11 units of distance which is covered in 169.11/v units of time (v is taken as the velocity of robot1).

$$\text{Distance of M from J3 is } \sqrt{(75.56 - 70)^2 + (68.95 - 30)^2} = 39.35 \text{ units}$$

Robot2 reached J3 covering a distance of 58.31 units

Objects	X	Y	Objects	X	Y	m	c			
J2	9	6	S1	20	100	8.5454545	-70.90909			
WITH										
R2	120	0	J3	70	30	-0.6	72	15.62642	62.624254	There is no collision
J3	70	30	S4	80	100	7	-460	-251.7647	-2222.352	There is no collision
S4	80	100	J1	99	77	-1.210526	196.84210	27.444825	163.61942	There is no collision
J1	99	77	S3	60	100	-0.589743	135.38461	22.582291	122.06685	There is no collision

Figure 9: Collision detection between J2S1 with R2J3, J3S4, S4J1 and J1S3.

Objects	X	Y	Objects	X	Y	m	c			
S1	20	100	J4	88	62	-0.558823	111.17647			
WITH										
R2	120	0	J3	70	30	-0.6	72	-951.4285	642.85714	There is no collision
J3	70	30	S4	80	100	7	-460	75.564202	68.949416	It cannot be concluded that there is no collision
S4	80	100	J1	99	77	-1.210526	196.84210	131.44893	37.719714	There is no collision
J1	99	77	S3	60	100	-0.589743	135.38461	782.92682	-326.3414	There is no collision

Figure 10: Collision detection between S1J4 with R2J3, J3S4, S4J1 and J1S3.

Objects	X	Y	Objects	X	Y	m	c			
J4	88	62	S2	40	100	-0.791666	131.66666			
WITH										
R2	120	0	J3	70	30	-0.6	72	311.30434	-114.7826	There is no collision
J3	70	30	S4	80	100	7	-460	75.935828	71.550802	It cannot be concluded that there is no collision
S4	80	100	J1	99	77	-1.210526	196.84210	155.60209	8.4816753	There is no collision
J1	99	77	S3	60	100	-0.589743	135.38461	-18.41263	146.24338	There is no collision

1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit

**Figure 11:** Collision detection between J4S2 with R2J3, J3S4, S4J1 and J1S3.

Objects	X	Y	Objects	X	Y	m	c			
R1	0	0	J4	25	83	3.32	0			
WITH										
R2	120	0	J1	107	5	-0.384615	46.153846	12.458471	41.362126	There is no collision
J1	107	5	S4	80	100	-3.518518	381.48148	55.784228	185.20363	There is no collision
S4	80	100	J2	114	69	-0.911764	172.94117	40.867389	135.67973	There is no collision
J2	114	69	S3	60	100	-0.574074	134.44444	34.525394	114.62431	There is no collision

1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit

**Figure 12:** Collision detection between R1J4 with R2J1, J1S4, S4J2 and J2S3.

(from Figure 2).

For reaching M, Robot 2 has to cover  $58.31 + 39.55 = 97.66$  units of distance which is covered in  $97.66/v$  units of time ( $v$  is taken as the velocity of robot2).

As  $97.66/v < 169.11/v$ , Robot2 passes through the point M much earlier than Robot1 and so there is no collision.

From Figure 10, it is found that the line S1-J4 will intersect the line S4-J1 at the point (131.44, 37.72) which does not lie within the points S1 and J4. So there is no collision.

The line S1-J4 will intersect the line J1-S3 at the point (782.93, -326.34) which does not lie within the points S1 and J4. So there is no collision.

From Figure 11, it is found that the line J4-S2 will intersect the line R2-J3 at the point (311.30, -114.78) which does not lie between the points R2 and J3. So there is no collision.

The line J4-S2 will intersect the line J3-S4 at the point (75.94, 71.55) which lies between the points J3 and S4 and between the points J4 and S2. So it cannot be concluded that there is no collision.

Let N be the point of intersection of J4-S2 and J3-S4. Location of N is (75.94, 71.55) (from Figure 11).

$$\text{Distance of N from J4 is } \sqrt{(75.94 - 88)^2 + (71.55 - 62)^2} = 15.38 \text{ units.}$$

Robot1 reached J4 covering a distance of 183.36 (from Figure 2).

Figure 2).

For reaching N, Robot1 has to cover  $183.36 + 15.38 = 198.74$  units of distance which is covered in  $198.74/v$  units of time ( $v$  is taken as the velocity of robot1).

$$\text{Distance of N from J3 is } \sqrt{(75.94 - 70)^2 + (71.55 - 30)^2} = 40.98 \text{ units.}$$

Robot2 reached J3 covering a distance of 58.31 (from Figure 2).

For reaching N, Robot2 has to cover  $58.31 + 40.98 = 99.29$  units of distance which is covered in  $99.29/v$  units of time ( $v$  is taken as the velocity of robot2).

As  $99.29/v < 198.74/v$ , Robot2 passes through the point N much earlier than Robot1 and so there is no collision.

From Figure 11, it is found that the line J4-S2 will intersect the line S4-J1 at the point (155.60, 8.48) which does not lie between the points J4 and S2. So there is no collision.

The line J4-S2 will intersect the line J1-S3 at the point (-18.41, 146.24) which does not lie between the points J4 and S2. So there is no collision.

### Demonstration of the algorithm with test case 2

From Figure 12, it is found that the line R1-J4 intersects the line R2-J1 at the point (12.46, 41.36) which is not between the points R2 and J1. So there is no collision.

The line R1-J4 intersects the line J1-S4 at the point (55.78,

185.20) which is not between the points J1 and S4. So there is no collision.

The line R1-J4 intersects the line S4-J2 at the point (40.87, 135.68) which is not between the points S4 and J2. So there is no collision.

The line R1-J4 intersects the line J2-S3 at the point (34.53, 114.62) which is not between the points J2 and S3. So there is no collision.

From Figure 13, it is found that the line J4-S1 intersects the line R2-J1 at the point (40.41, 30.61) which is not between the points R2 and J1. So there is no collision.

The line J4-S1 intersects the line J1-S4 at the point (1801.25, -5956.25) which is not between the points J1 and S4. So there is no collision.

The line J4-S1 intersects the line S4-J2 at the point (-1.99, 174.75) which is not between the points S4 and J2. So there is no collision.

The line J4-S1 intersects the line J2-S3 at the point (11.87, 127.63) which is not between the points J2 and S3. So there is no collision.

From Figure 14, it is found that the line S1-J3 intersects the line R2-J1 at the point (146.90, -10.34) which is not between the points R2 and J1. So there is no collision.

The line S1-J3 intersects the line J1-S4 at the point (99.70, 30.70) which is not between the points S1 and J3. So there is

no collision.

The line S1-J3 intersects the line S4-J2 at the point (1316.36, -1027.27) which is not between the points S4 and J2. So there is no collision.

The line S1-J3 intersects the line J2-S3 at the point (-57.71, 167.57) which is not between the points J2 and S3. So there is no collision.

From Figure 15, it is found that the line J3-S2 intersects the line R2-J1 at the point (51.02, 26.53) which is not between the points R2 and J1. So there is no collision.

The line J3-S2 intersects the line J1-S4 at the point (-4.71, 398.04) which is not between the points J1 and S4. So there is no collision.

The line J3-S2 intersects the line S4-J2 at the point (33.66, 142.25) which is not between the points S4 and J2. So there is no collision.

The line J3-S2 intersects the line J2-S3 at the point (38.12, 112.56) which is not between the points J2 and S3. So there is no collision.

### Demonstration of the algorithm with test case 3

From Figure 16, it is observed that the line R1-J4 intersects with the line R2-J2 at (91.79, 43.60) which is not between the points R1 and J4. So there is no collision.

The line R1-J4 intersects with the line J2-S4 at (71.76,

Objects	X	Y	Objects	X	Y	m	c			
J4	25	83	S1	20	100	-3.4	168			
WITH										
R2	120	0	J1	107	5	-0.384615	46.153846	X	Y	Decision
J1	107	5	S4	80	100	-3.518518	381.48148	40.408163	30.612244	There is no collision
S4	80	100	J2	114	69	-0.911764	172.94117	1801.25	-5956.249	There is no collision
J2	114	69	S3	60	100	-0.574074	134.44444	-1.985815	174.75177	There is no collision
								11.874180	127.62778	There is no collision
<div>1st Solution</div> <div>2nd Solution</div> <div>3rd Solution</div> <div>4th Solution</div> <div>Refresh</div> <div>Quit</div>										

**Figure 13:** Collision detection between J4S1 with R2J1, J1S4, S4J2 and J2S3.

Objects	X	Y	Objects	X	Y	m	c			
S1	20	100	J3	43	80	-0.869565	117.39130			
WITH										
R2	120	0	J1	107	5	-0.384615	46.153846	X	Y	Decision
J1	107	5	S4	80	100	-3.518518	381.48148	146.89655	-10.34482	There is no collision
S4	80	100	J2	114	69	-0.911764	172.94117	99.696048	30.699088	There is no collision
J2	114	69	S3	60	100	-0.574074	134.44444	1316.3636	-1027.272	There is no collision
								-57.71117	167.57493	There is no collision
<div>1st Solution</div> <div>2nd Solution</div> <div>3rd Solution</div> <div>4th Solution</div> <div>Refresh</div> <div>Quit</div>										

**Figure 14:** Collision detection between S1J3 with R2J1, J1S4, S4J2 and J2S3.

Objects	X	Y	Objects	X	Y	m	c		
J3	43	80	S2	40	100	-6.666666	366.66666		
WITH									
R2	120	0	J1	107	5	-0.384615	46.153846	51.020408	26.530612
J1	107	5	S4	80	100	-3.518518	381.48148	4.705882	398.03921
S4	80	100	J2	114	69	-0.911764	172.94117	33.662691	142.24872
J2	114	69	S3	60	100	-0.574074	134.44444	38.115501	112.56332
Decision									
									There is no collision
									There is no collision
									There is no collision
									There is no collision
1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit									

Figure 15: Collision detection between J3S2 with R2J1, J1S4, S4J2 and J2S3.

Objects	X	Y	Objects	X	Y	m	c		
R1	0	0	J4	40	19	0.475	0		
WITH									
R2	120	0	J2	76	68	-1.545454	185.45454	91.788526	43.599550
J2	76	68	S4	80	100	8	-540	71.760797	34.086378
S4	80	100	J1	56	88	0.5	60	-2400	-1140
J1	56	88	S3	60	100	3	-80	31.683168	15.049504
Decision									
									There is no collision
									There is no collision
									There is no collision
									There is no collision
1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit									

Figure 16: Collision detection between R1J4 with R2J2, J2S4, S4J1 and J1S3.

Objects	X	Y	Objects	X	Y	m	c		
J4	40	19	S2	40	100				
WITH									
R2	120	0	J2	76	68	-1.545454	185.45454	40	123.63636
J2	76	68	S4	80	100	8	-540	40	-220
S4	80	100	J1	56	88	0.5	60	40	80
J1	56	88	S3	60	100	3	-80	40	40
Decision									
									There is no collision
									There is no collision
									There is no collision
									There is no collision
1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit									

Figure 17: Collision detection between J4S2 with R2J2, J2S4, S4J1 and J1S3.

34.09) which is not between the points R1 and J4. So there is no collision.

The line R1-J4 intersects with the line S4-J1 at (-2400, -1140) which is not between the points R1 and J4. So there is no collision.

The line R1-J4 intersects with the line J1-S3 at (31.68, 15.05) which is not between the points J1 and S3. So there is no collision.

From Figure 17, it is observed that the line J4-S2 is a straight line parallel to the y-axis. So m could not be calculated. It intersects with the line R2-J2 at (40, 123.64) which is not

between the points R2 and J2. So there is no collision.

The line J4-S2 intersects with the line J2-S4 at (40, -220) which is not between the points J2 and S4. So there is no collision.

The line J4-S2 intersects with the line S4-J1 at (40, 80) which is not between the points S4 and J1. So there is no collision.

The line J4-S2 intersects with the line J1-S3 at (40, 40) which is not between the points J1 and S3. So there is no collision.

From Figure 18, it is observed that the line S2-J3 intersects

Objects	X	Y	Objects	X	Y	m	c			
S2	40	100	J3	50	58	4.2	268			
WITH										
R2	120	0	J2	76	68	-1.545454	185.45454	31.095890	137.39726	Decision
J2	76	68	S4	80	100	8	-540	66.229508	-10.16393	There is no collision
S4	80	100	J1	56	88	0.5	60	44.255319	82.127659	There is no collision
J1	56	88	S3	60	100	3	-80	48.333333	65	There is no collision

1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit

**Figure 18:** Collision detection between S2J3 with R2J2, J2S4, S4J1 and J1S3.

Objects	X	Y	Objects	X	Y	m	c			
J3	50	58	S1	20	100	-1.4	128			
WITH										
R2	120	0	J2	76	68	-1.545454	185.45454	395	-425	Decision
J2	76	68	S4	80	100	8	-540	71.063829	28.510638	There is no collision
S4	80	100	J1	56	88	0.5	60	35.789473	77.894736	There is no collision
J1	56	88	S3	60	100	3	-80	47.272727	61.818181	There is no collision

1st Solution 2nd Solution 3rd Solution 4th Solution Refresh Quit

**Figure 19:** Collision detection between J3S1 with R2J2, J2S4, S4J1 and J1S3.

with the line R2-J2 at (31.10, 137.40) which is not between the points R2 and J2. So there is no collision.

The line S2-J3 intersects with the line J2-S4 at (66.23, -10.16) which is not between the points J2 and S4. So there is no collision.

The line S2-J3 intersects with the line S4-J1 at (44.26, 82.13) which is not between the points S4 and J1. So there is no collision.

The line S2-J3 intersects with the line J1-S3 at (48.33, 65) which is not between the points J1 and S3. So there is no collision.

From Figure 19, it is observed that the line J3-S1 intersects with the line R2-J2 at (395, -425) which is not between the points R2 and J2. So there is no collision.

The line J3-S1 intersects with the line J2-S4 at (71.06, 28.51) which is not between the points J2 and S4. So there is no collision.

The line J3-S1 intersects with the line S4-J1 at (35.79, 77.89) which is not between the points S4 and J1. So there is no collision.

The line J3-S1 intersects with the line J1-S3 at (47.27, 61.82) which is not between the points J1 and S3. So there is no collision.

## Conclusion

In this work, task planning for transportation of multiple objects by dual robots has been considered. A new algorithm

has been developed for finding the routes for the robots in overall shortest possible time and another new algorithm has been developed to find out whether there is any collision between the two robots or not. As the robots are assumed to move with constant and same velocities, the distances covered by the robots are directly related to the time of movement of the robots. The algorithms have been implemented with different cases of object locations.

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